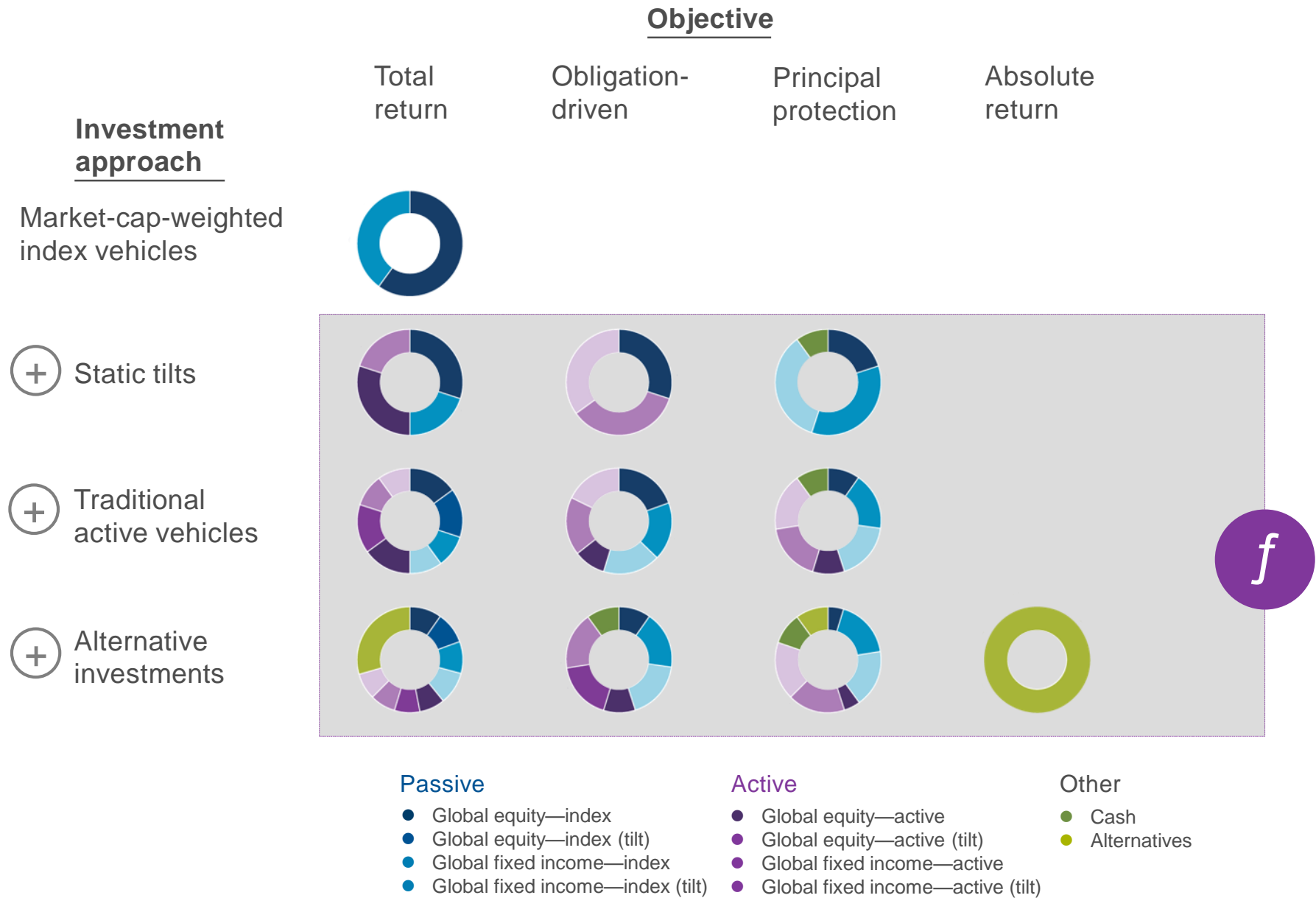


Quantitative Investment: From indexing to factor investing



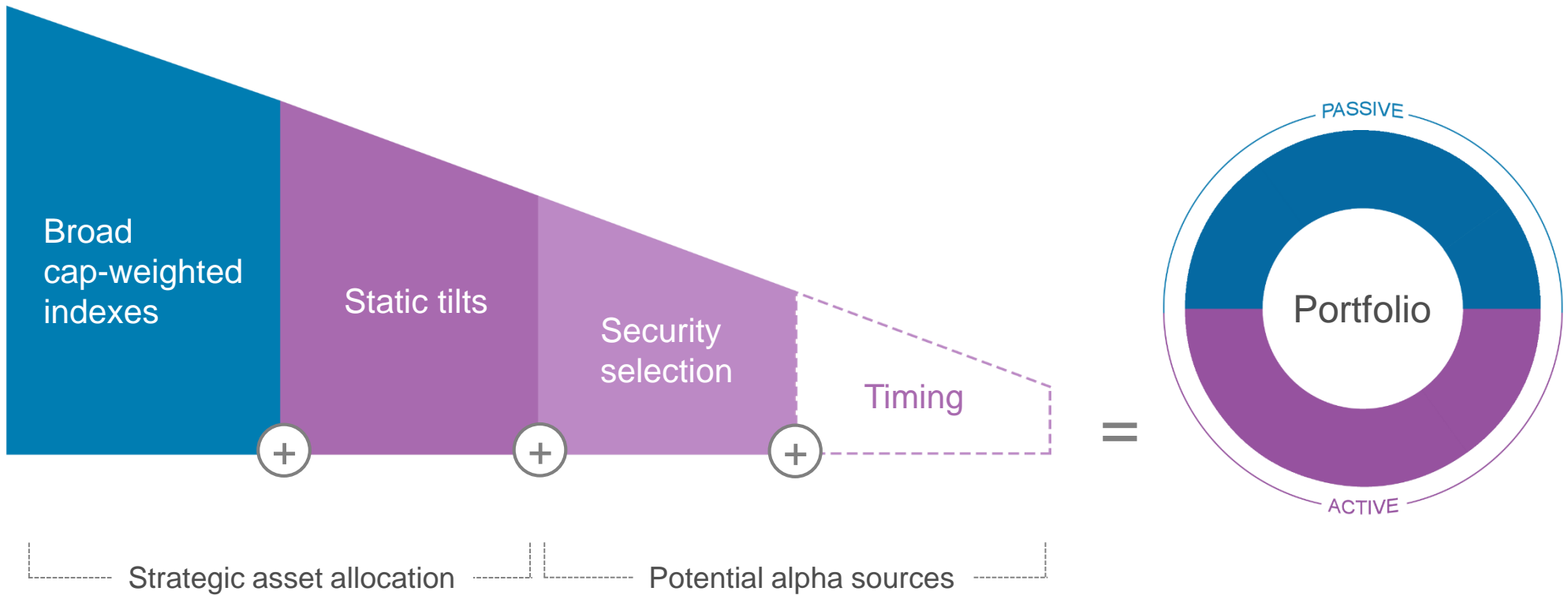
Vanguard

What's the prudent portfolio mix? It depends



Notes: The allocations in each pie chart are for purposes of illustration only and are not intended as specific recommendations. Any actual portfolio recommendations would be determined using investor-specific criteria. For more on this topic, see the Vanguard research paper *A Framework for Institutional Portfolio Construction*, 2016. Source: Vanguard.

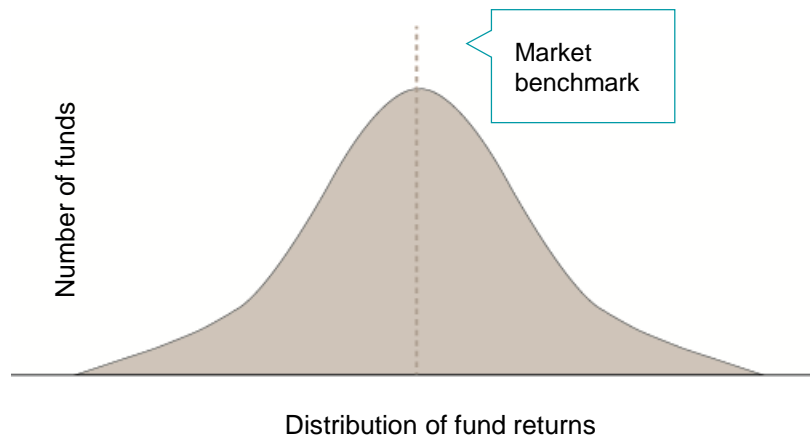
A framework for portfolio construction



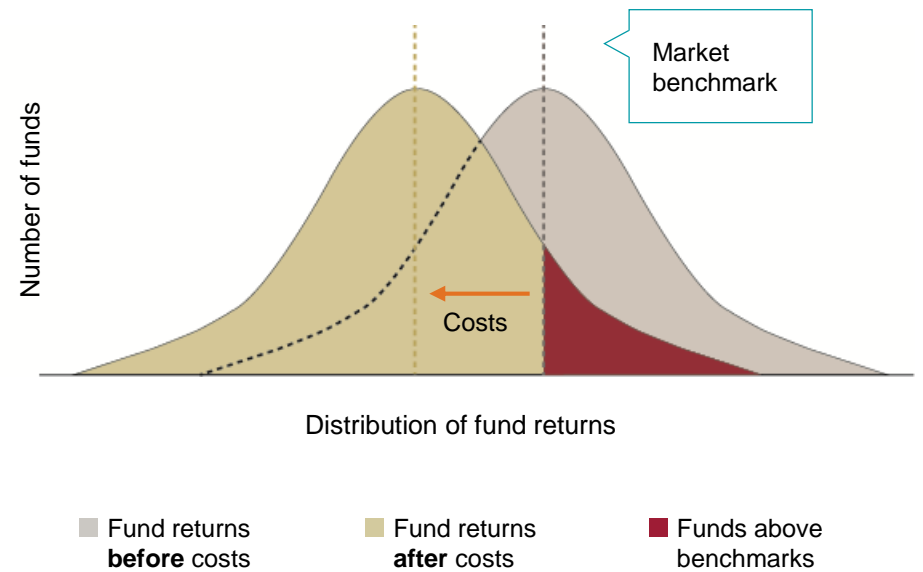
Quantitative investing: Indexing

The key to indexing: Low costs

- Investing is a zero-sum game before costs



- Investing is a negative-sum game after costs



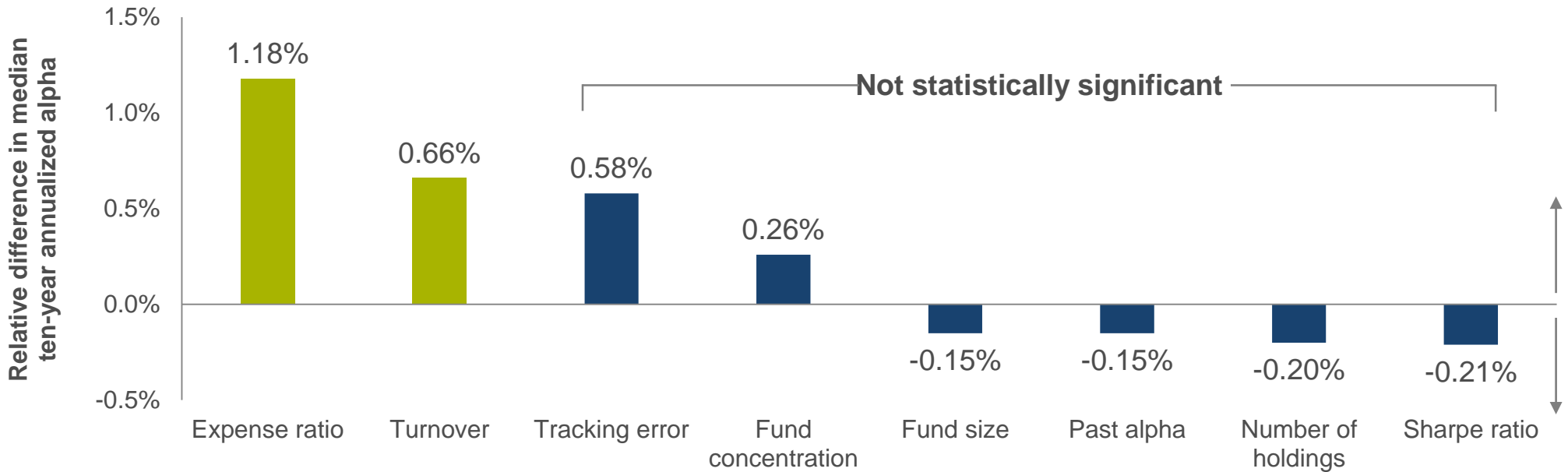
The holdings of all investors aggregate to form a market. Outperformance by one investor necessarily means underperformance by another.

After costs, a majority of investors will underperform the market benchmark. The key to long-term, consistent success is low-cost investing.



Is there an ex-ante metric that can improve the odds?

Cost is a powerful indicator of future alpha



↑ Median of lowest-quartile metric funds outperformed
↓ Median of highest-quartile metric funds outperformed

Notes: The bars represent the difference in the median annual alpha from January 1, 2006, through December 31, 2016, of mutual funds in the lowest and highest quartiles, based on the above metric measurements from January 1, 2004, through December 31, 2006. Fund concentration is measured as the percentage of assets in the top ten holdings. The expense ratio and turnover were the only variables significant at the 99% confidence level. For more information, see the Vanguard research note *Shopping for Alpha: You Get What You Don't Pay For*, 2015.
Sources: Vanguard calculations, based on data from Morningstar, Inc., and Fama-French factor data.

Tracking the indexes

Steps to keep our portfolios on track with benchmarks

- Proprietary system designed to neutralize the major risk factors
- Limit orders help minimize transaction costs
- Futures contracts help provide liquidity
- Portfolio holdings rebalanced daily
- Cash positions equitized daily



Comprehensive risk assessment

- Vanguard exercises ongoing rigorous risk control

Individual stock level

Daily evaluation of security weights relative to the index

Factor level

Daily monitoring of sector weights, market capitalization, volatility, and style relative to the index

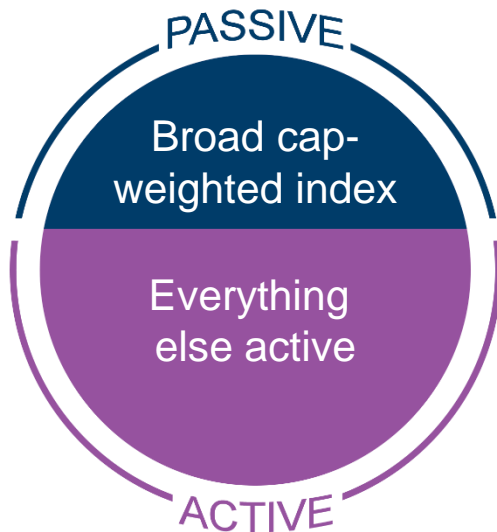
Portfolio level

Daily analysis of portfolio characteristics and ongoing rebalancing to match benchmark characteristics

Sample imbalance report for individual holdings

Ticker	Shares held	Recent price	Market value	Portfolio wt.	Index wt.	% Imbalance	Dollar imbalance	Share imbalance
SPG	2,425,936	36.780	\$89,225,926	0.12977	0.12808	-0.00169	-1,162,840	-31,700
MCO	1,838,772	23.410	\$43,045,653	0.06260	0.06167	-0.00093	-639,270	-27,400
RHI	1,468,728	18.900	\$27,758,959	0.04037	0.03956	-0.00081	-558,419	-29,600
GWW	612,161	73.600	\$45,055,050	0.06553	0.06476	-0.00077	-527,711	-7,200
ALTR	2,815,015	18.400	\$51,796,276	0.07533	0.07463	-0.00070	-484,199	-26,400
CI	2,603,008	18.640	\$48,520,069	0.07057	0.06986	-0.00070	-482,218	-25,900
DRI	1,313,981	37.010	\$48,630,437	0.07073	0.07011	-0.00062	-423,549	-11,500

Quantitative investing: factors



Active investing is any investment strategy that is not broad market-cap-weighted.

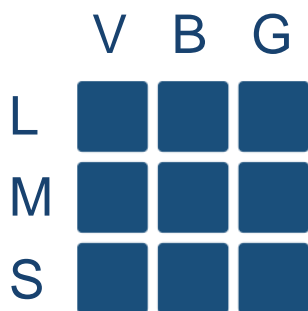


Factors are the DNA of an investment portfolio.

They are the underlying characteristics that explain and influence an investment's risk.

Equity factor-based investing is a systematic, diversified, and disciplined form of active management that intentionally targets consistent exposure to one or more well-known factors that have reasonable odds of helping an investor meet an objective.

Equity exposure should be evaluated through different lenses



Style



Location



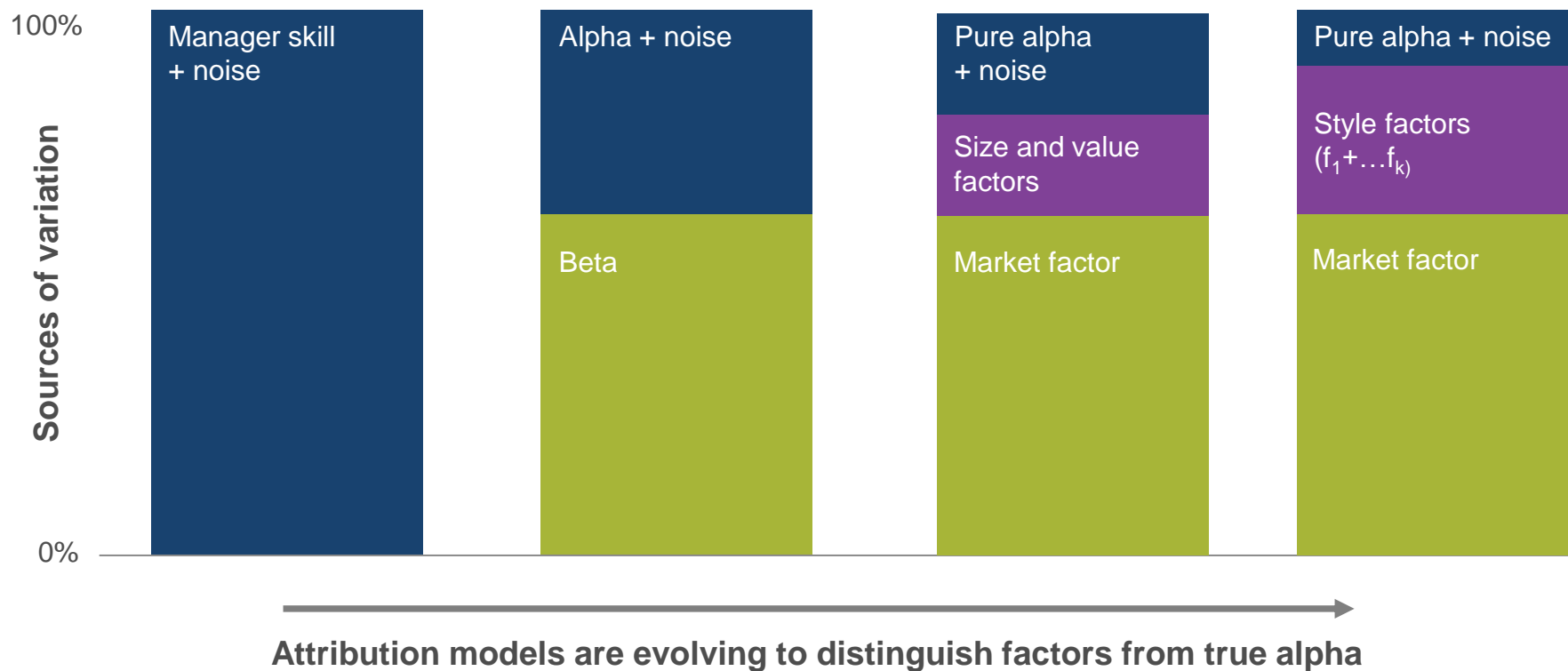
Sectors



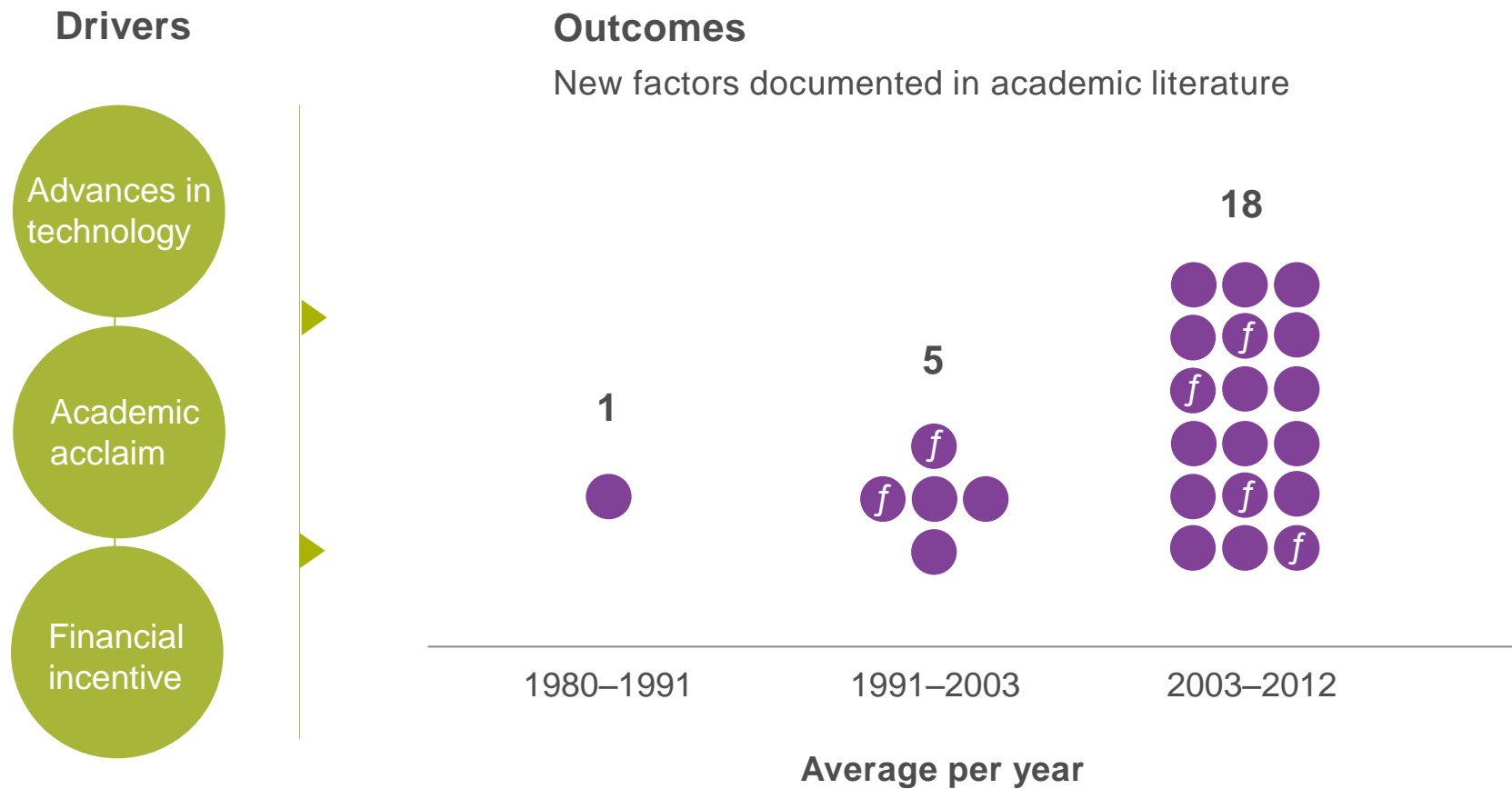
Factor

Factors are raising the bar for traditional active management

Advances in research and technology and low-cost factor vehicles are raising the bar for traditional active management

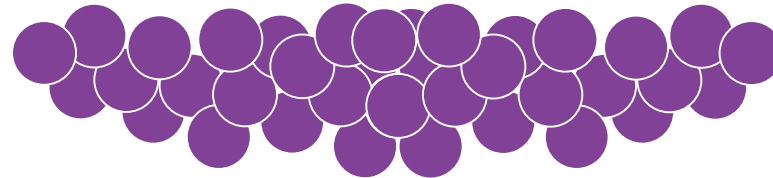


Equity factors that supposedly generate excess return have proliferated



Which, if any, may benefit investors in the future?

300+ documented
characteristics today



**Enduring
logical rationale**
Risk-based and/or
behavioral reason(s)

**Extensive
empirical evidence**
Out-of-sample tests,
breadth of academic
studies, etc.

Investability
Real-world
implementation costs



“Academic” results don’t equal real-world portfolio results

Academic papers often . . .

Test long/short, not
long-only strategies

Ignore management
and oversight
expenses

Disregard transaction-
related costs

Relative performance has been inconsistent over the short term

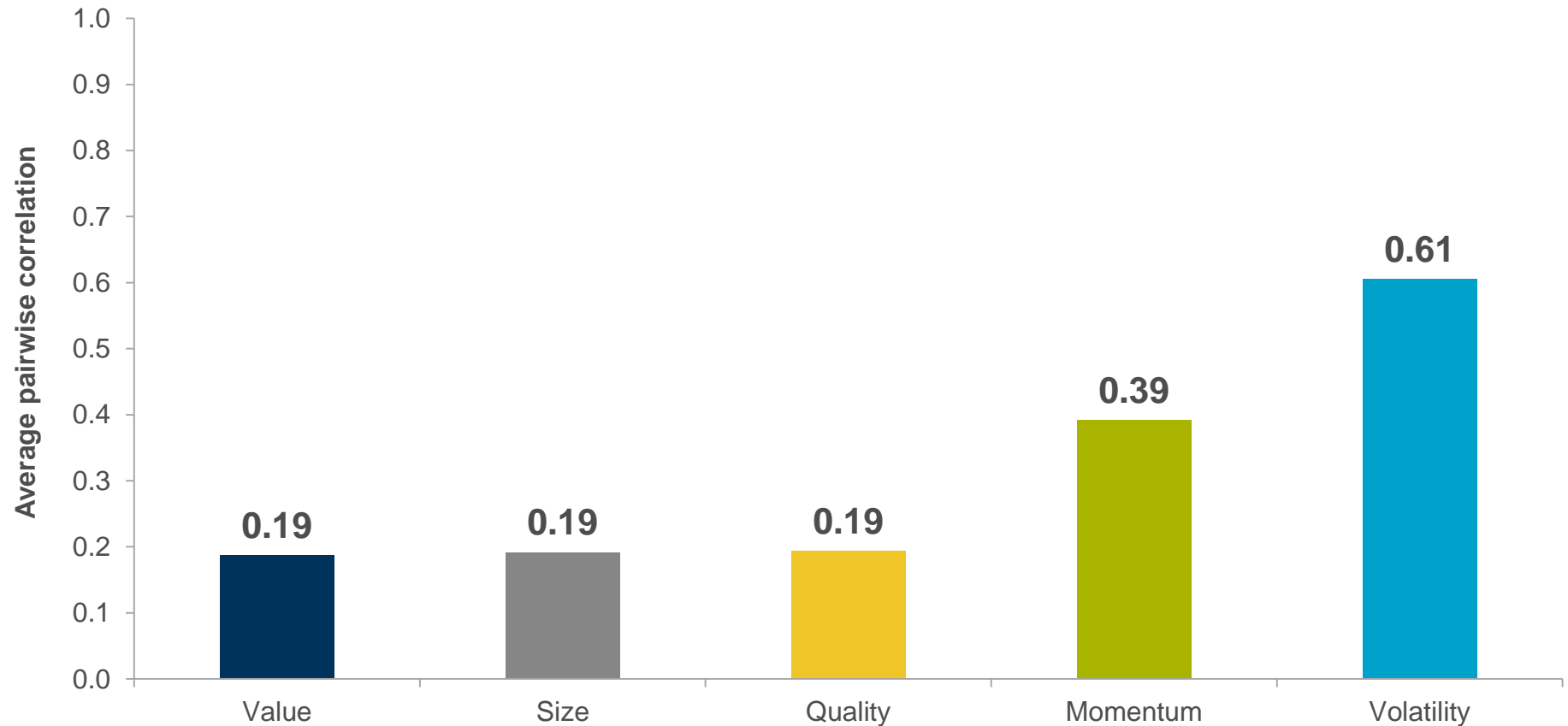


Notes: Data cover January 1, 2002, through December 31, 2015. Excess returns are calculated relative to the MSCI World Total Return Index (USD). This figure includes back-tested index performance. For information regarding index inception and index-live dates, please see the table in the Appendix.

Sources: Vanguard calculations, using data from Thomson Reuters Datastream, MSCI, Bloomberg, and FTSE.

Diversifying factor exposure globally can yield benefits

Correlation of equity factor tilt excess returns versus local market indexes (in USD)



Notes: All calculations cover monthly excess returns from December 31, 2001, through May 31, 2016, except for the volatility factor, which covers November 30, 2002, through May 31, 2016. Country factor indexes included in the analysis are for the United States, United Kingdom, and Japan.

Sources: Vanguard calculations, based on data from Thomson Reuters Datastream and MSCI.

Single or multifactor? Low correlation of excess returns can diversify active risk

Correlation of monthly excess returns, 2002–2016

	Value	Quality	Volatility	Momentum	Size	Liquidity
Value						
Quality	-0.59					
Volatility	-0.38	0.49				
Momentum	-0.11	0.37	0.37			
Size	0.43	-0.30	-0.15	0.10		
Liquidity	0.57	-0.44	-0.13	0.08	0.63	

■ High: > 0.7
 ■ Medium: 0.3–0.7
 ■ Low: < 0.3

Notes: Data cover December 31, 2001, through September 30, 2016. Excess returns are calculated relative to the MSCI World Total Return Index (USD). This figure includes back-tested index performance. For information regarding index inception and index-live dates, please see the table in the Appendix.

Sources: Vanguard calculations, using data from Thomson Reuters Datastream, MSCI, Bloomberg, and FTSE.

What are your goals? Your path forward

Enhance return

Generate excess returns using a static tilt to a particular factor

Reduce risk

Lessen total volatility with a minimal reduction in return

Substitution

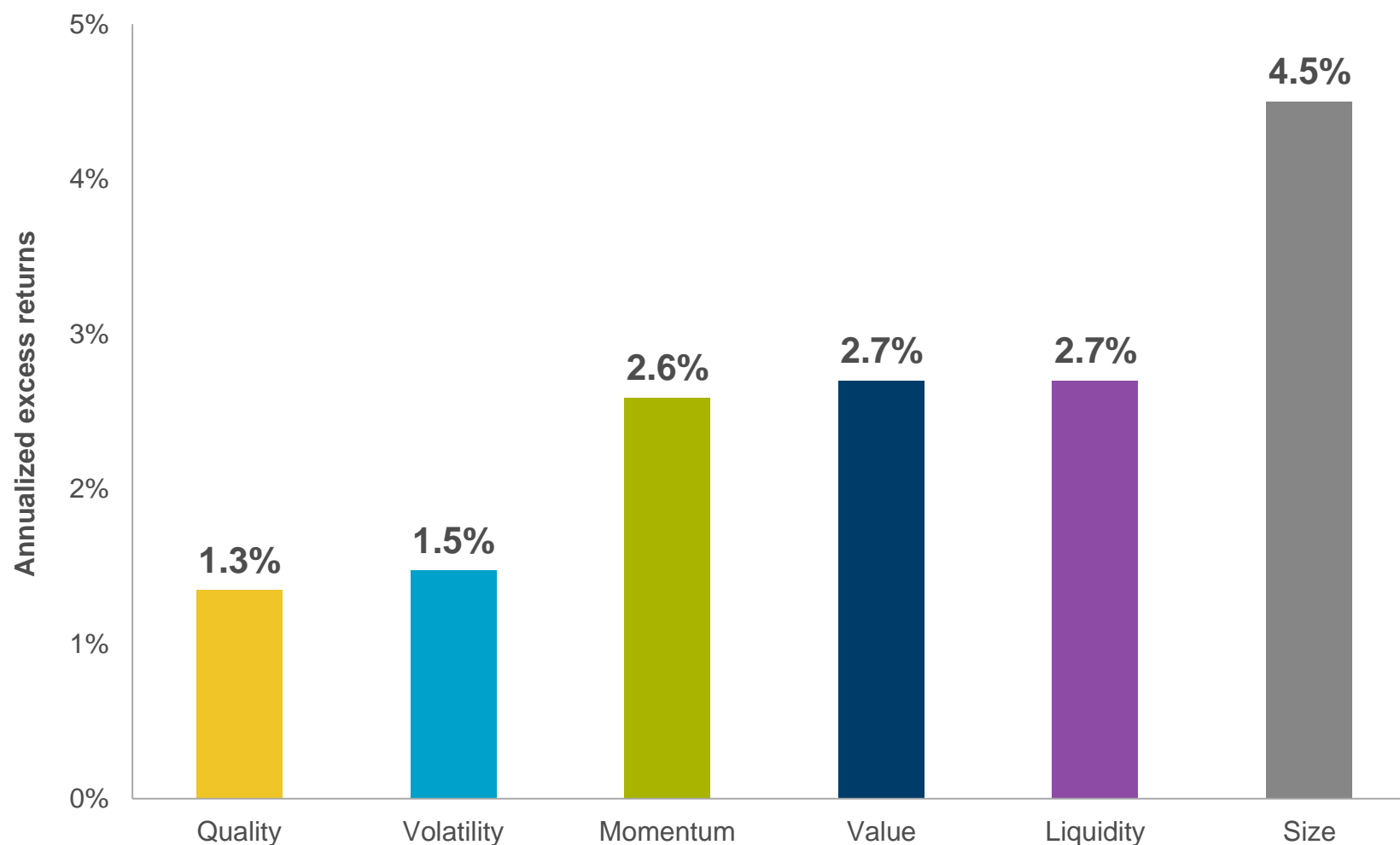
Represent a high-cost active manager's returns with a broad market index vehicle paired with one or more low-cost, factor-tilted equity products

Completion

Adjust a factor over/underweight within the portfolio by allotting assets to a factor-tilted strategy

Role option 1: Static tilt—Enhance return

Numerous equity factor tilts have outperformed historically

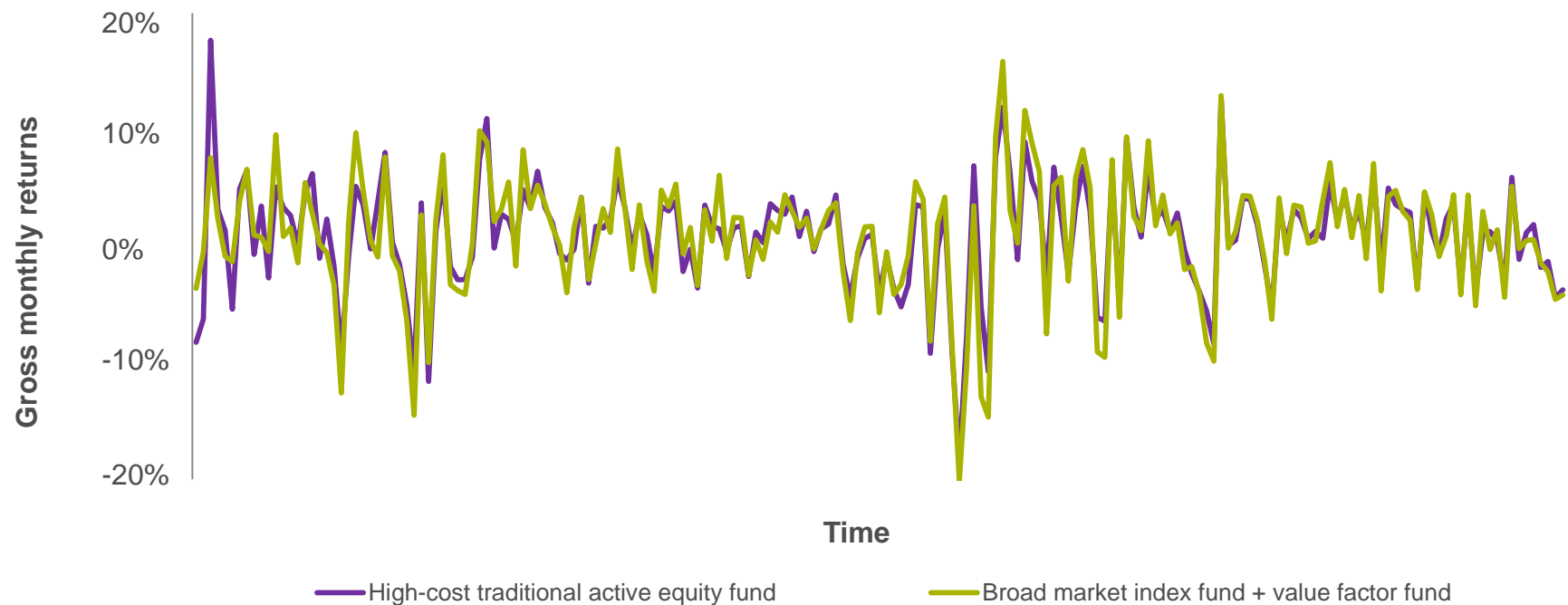


Notes: All results are as of September 30, 2016. Excess returns are calculated relative to the MSCI World Total Return Index (USD). MSCI World Momentum Index (USD) history begins May 31, 1973; MSCI World Value Index (USD) is from December 31, 1974, to November 30, 1997, and MSCI World Enhanced Value Index thereafter; MSCI World Quality Index (USD) begins November 30, 1975; MSCI World Minimum Volatility Index (USD) begins May 31, 1988; MSCI World Small Cap Index (USD) begins December 31, 2000; and FTSE Developed Illiquidity Factor Index (USD) begins September 30, 2001. This figure includes back-tested index performance. For information regarding index inception and index-live dates, please see the table in the Appendix.

Sources: Vanguard calculations, using data from Thomson Reuters Datastream, MSCI, Bloomberg, and FTSE.

Role option 3: High-cost traditional active manager substitution

Step 2: Try to represent the manager's performance while reducing costs



Conclusion

A form of active management

- Greater transparency
- More control
- Lower cost

Key considerations

- Persistence rationale
- Portfolio construction and implementation trade-offs
- Cost

Suitability depends on:

- Investment objectives
- Risk tolerance
- Due diligence capabilities